Lecture Notes 3 Econ 29000, Principles of Statistics Kevin R Foster, CCNY Spring 2011

Last class talked about correlations. We usually want to know not just about correlation but also about causation, but those are not the same thing. The problem can be stated, using logical terminology, that correlation does not imply causation, but causation does imply correlation. We observe only correlations, though. Many examples...

More examples of correlation:

It is common in finance to want to know the correlation between returns on different assets.

First remember the difference between the returns and the level of an asset or index!

An investment in multiple assets, with the same return but that are uncorrelated, will have the same return but with less overall risk. We can show this on Excel; first we'll do random numbers to show the basic idea and then use specific stocks.

How can we create normally-distributed random numbers in Excel? RAND() gives random numbers between zero and one; NORMSINV(RAND()) gives normally distributed random numbers. (If you want variables with other distributions, use the inverse of those distribution functions.) Suppose that two variables each have returns given as 2% + a normally-distributed random number; this is shown in Excel sheet, lecturenotes3.xls

With finance data, we use the return not just the price. This is because we assume that investors care about returns per dollar not the level of the stock price.

Important Questions:

- When we calculate a correlation, what number is "big"? Will see random errors what amount of evidence can convince us that there is really a correlation?
- When we calculate conditional means, and find differences between groups, what difference is "big"? What amount of evidence would convince us of a difference?

To answer these, we need to think about randomness – in other perceptual problems, noise, blur.

Learning Outcomes (from CFA exam Study Session 2, Quantitative Methods) Students will be able to:

 calculate and interpret relative frequencies, given a frequency distribution, and describe the properties of a dataset presented as a histogram;

- define, calculate, and interpret measures of central tendency, including the population mean, sample mean, median, and mode;
- define, calculate, and interpret measures of variation, including the population standard deviation and the sample standard deviation;
- define and interpret the covariance and correlation;
- define a random variable, an outcome, an event, mutually exclusive events, and exhaustive events;
- distinguish between dependent and independent events;

Probability

Beyond presenting some basic measures such as averages and standard deviations, we want to try to understand how much these measures can tell us about the larger world. How likely is it, that we're being fooled, into thinking that there's a relationship when actually none exists? To think through these questions we must consider the logical implications of randomness and often use some basic statistical distributions (discrete or continuous).

Think Like a Statistician

The basic question that a Statistician must ask is "How likely is it, that I'm being fooled?" Once we accept that the world is random (rather than a manifestation of some god's will), we must decide how to make our decisions, knowing that we cannot guarantee that we will always be right. There is some risk that the world will seem to be one way, when actually it is not. The stars are strewn randomly across the sky but some bright ones seem to line up into patterns. So too any data might sometimes line up into patterns.

Statisticians tend to stand on their heads and ask, suppose there were actually no relationship? (Sometimes they ask, "suppose the conventional wisdom were true?") This statement, about "no relationship," is called the **Null Hypothesis**, sometimes abbreviated as H_o. The Null Hypothesis is tested against an **Alternative Hypothesis**, H_A.

Before we even begin looking at the data we can set down some rules for this test. We know that there is some probability that nature will fool me, that it will seem as though there is a relationship when actually there is none. The statistical test will create a model of a world where there is actually no relationship and then ask how likely it is that we could see what we actually see, "How likely is it, that I'm being fooled?" What if there were actually no relationship, is there some chance that I could see what I actually see?

Randomness in Sports

As an example, consider sports events. As any sports fan knows, a team or individual can get lucky or unlucky. The baseball World Series, for example, has seven games. It is designed to ensure that, by the end, one team or the other wins. But will the better team always win?

First make a note about subjectivity: if I am a fan of the team that won, then I will be convinced that the better team won; if I'm a fan of the losing team then I'll be certain that the better team got unlucky. But fans of each team might agree, if they discussed the question before the Series were played, that luck has a role.

Will the better team win? Clearly a seven-game Series means that one team or the other will win, even if they are exactly matched (if each had precisely a 50% chance of winning). If two representatives tossed a coin in the air seven times, then one or the other would win at least four tosses – maybe even more. We can use a computer to simulate seven coin-tosses by having it pick a random number between zero and one and defining a "win" as when the random number is greater than 0.5.

Or instead of having a computer do it, we could use a bit of statistical theory.

Some math

Suppose we start with just one coin-toss or game (baseball uses 7 games to decide a champion; football uses just one). Choose to focus on one team so that we can talk about "win" and "loss". If this team has a probability of winning that is equal to *p*, then it has a probability of losing equal to (1-*p*). So even if p, the probability of winning, is equal to 0.6, there is still a 40% chance that it could lose a single game. In fact unless the probability of winning is 100%, there is some chance, however remote, that the lesser team will win.

What about if they played two games? What are the outcomes? The probability of a team winning both games is $p*p = p^2$. If the probability were 0.5 then the probability of winning twice in a row would be 0.25.

A table can show this:

	Win Game 1 {p}	Lose Game 1 {1-p}
Win Game 2 {p}	outcome: W,W	L,W
Lose Game 2 {1-p}	W,L	L,L

This is a fundamental fact about how probabilities are represented mathematically: if the probabilities are not related (i.e. if the tossed coin has no memory) then the probability of both events happening is found my multiplying the probabilities of each individual outcome. (What if they're not unrelated, you may ask? What if the first team that wins gets a psychological boost in the next so they're more likely to win the second game? Then the math gets more complicated – we'll come back to that question!)

The math notation for two events, call them A and B, both happening is: $Pr\{A \text{ and } B\} = Pr\{A \cap B\}$

The fundamental fact of independence is then represented as: $Pr \{A \cap B\} = Pr \{A\} Pr \{B\}$ *if A and B are independent* where we use the term "independent" for when there is no relationship between them.

The probability that a team could lose both games is $(1-p)*(1-p) = (1-p)^2$. The probability that the teams could split the series (each wins just one) is p*(1-p) + (1-p)*p = 2p(1-p). There are two ways that each team could win just one game: either the series splits (Win,Loss) or (Loss,Win).

For three games the outcomes become more complicated: now there are 8 combinations of win and loss:

(W,W,W)	(W,W,L)	(W,L,W)	(L,W,W)	(W,L,L)	(L,W,L)	(L,L,W)	(L,L,L)
p*p*p	p*p*(1-p)	р*(1-р)р	(1-p)p*p	р(1-р)(1-р)	(1-p)p(1-p)	(1-p)(1-p)p	(1-p)(1-p)(1-p)

and the probabilities are in the row below.

The team will win the series in any of the left-most 4 outcomes so its overall probability of winning the series is

 $p^{3}+3p^{2}(1-p)$

while its probability of losing the series is

$$3p(1-p)^{2}+(1-p)^{3}$$
.

Clearly if p is 0.5 so that p=(1-p) then the chances of either team winning the three-game series are equal. If the probabilities are not equal then the chances are different, but as long as there is a probability not equal to one or zero (i.e. no certainty) then there is a chance that the worse team could win.

If you keep on working out the probabilities for longer and longer series you might notice that the coefficients and functional forms are right out of Pascal's Triangle. This is your first notice of just how "normal" the Normal Distribution is, in the sense that it jumps into all sorts of places where you might not expect it. The terms of Pascal's Triangle begin (as N becomes large) to have a normal distribution! We'll come back to this again...

Terms and Definitions

Some basics: a sample space is the entire list of possible outcomes (can be whole long list or even mathematical sets such as real numbers); events are subsets of the sample space. Simple event is a single outcome (one dice comes up 6); a compound event is several outcomes (both dice come up 6). Notate an event as A. The complement of the event is the set of all events that are not in A; this is A'.

The events must be **mutually exclusive and exhaustive**, so a good deal of the hard work in probability is just figuring out how to list all of the events.

Mutually exclusive means that the events must be clearly defined so that the data observed can be classified into just one event. Exhaustive means that every possible data observed must fit into some event. The "mutually exclusive" part means that probabilities can be added up, so

that if the probability of rolling a "1" on a dice is 1/6 and the probability of rolling a 6 is 1/6, then the probability of rolling either a 1 or 6 is 2/6 = 1/3. The "exhaustive" part of defining the events means that the sum of all the events must equal one.

For example, suppose we roll two dice. We might want to think of "die #1 comes up as 6" as one event [in English, the singular of "dice" is "die" – how morbid gambling can be!]. But the other die can have 6 different values without changing the value of the first die. So a better list of events would be the integers from 2 to 12, the sum of the dice values – with the note that there are many ways of achieving some of the events (a 7 is a 6 &1 or a 5&2, or 4&3, or 3&4, or 2&5, or 1&6) while other events have only one path (each die comes up 6 to make 12).

A **sample space** is the set of all possible events. The sum of the probability of all of the events in the sample space is equal to one. There is a 100% chance that something happens (provided we've defined the sample space correctly). So if a lottery brags that there is a 2% chance that "you might be a winner!" this is equivalent to stating that there is a 98% chance that you'll lose.

Events have **probability**; this must lie between zero and one (inclusive); so $0 \le P \le 1$. The probability of all of the events in the sample space must sum to one. This means that the probability of an event and its complement must sum to one: $P\{A\} + P\{A'\} = 1$.

Probabilities come from empirical results (relative frequency approach) or the classical (a priori or postulated) assignment or from subjective beliefs that people have.

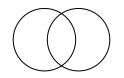
In empirical approach, the **Law of Large Numbers** is important: as the number of identical trials increases, the estimated frequency approaches its theoretical value. You can try flipping coins and seeing how many come up heads (*flip a bunch at a time to speed up the process*); it should be 50%.

We are often interested in finding the probability of two events both happening; this is the "intersection" of two events; the logical "and" relationship; two things both occurring. In the ATUS data we might want to find how many females have a college degree; in poker we might care about the chance of an opponent having an ace as one of her hole cards and the dealer turning up a king. We notate the intersection of A and B as $A \cap B$ and want to find $P\{A \cap B\}$. In SPSS this is notated with "&".

The "**union**" of two events is the logical "or" so it is either of two events occurring; this is $A \cup B$ so we might consider $P\{A \cup B\}$ or, in SPSS, "|". In the ATUS data we might want to combine people who report themselves as having race "black" with those who report "black – white".

Married people can buy life insurance policies that pay out either when the first person dies or after both die – logical and vs or.

Venn Diagrams (Ballantine)



General Law of Addition $P\{A \cup B\} = P\{A\} + P\{B\} - P\{A \cap B\}$ and so $P\{A \cap B\} = P\{A\} + P\{B\} - P\{A \cup B\}$

Mutually Exclusive (Special Law of Addition), If $A \cap B = \phi$ then $P\{A \cap B\} = 0$ and $P\{A \cup B\} = P\{A\} + P\{B\}$

Conditional Probability

 $P\{A|B\} = \frac{P\{A \cap B\}}{P\{B\}}$ if $P\{B\} \neq 0$. See Venn Diagram.

Independent Events

A is independent of B if and only if $P\{A|B\} = P\{A\}$

If we have multiple random variables then we can consider their **Joint Distribution**: the probability associated with each outcome in both sample spaces. So a coin flip has a simple discrete distribution: a 50% chance of heads and a 50% chance of tails. Flipping 2 coins gives a joint distribution: a 25% chance of both coming up heads, a 25% chance of both coming up tails, and a 50% chance of getting one head and one tail.

The probability of multiple independent events is found by multiplying the probabilities of each event together. So the chance of rolling two 6 on two dice is $\frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36}$. The probability of getting to the computer lab on the 6th floor of NAC from the first floor, without having to walk up a broken escalator, can be found this way too. Suppose the probability of an escalator not working is p; then the probability of it working is (1-p) and the probability of five escalators each working is $(1-p)^5$. So even if the probability of a breakdown is small (5%), still the probability of having every escalator work is just

$$(1-5\%)^5 = (95\%)^5 = (0.95)^5 = (\frac{95}{100})^5 = 0.7738 = 77.38\%$$
 so this implies that you'd expect to

walk more than once a week.

A simple representation of the joint distribution of two coin flips is a table:

_	coin 1 Heads	coin 1 Tails
coin 2 Heads	H,H at 25%	H,T at 25%

coin 2 Tails T,H at 25% T,T at 25% Where, since the outcomes are independent, we can just multiply the probabilities.

The Joint Distribution tells the probabilities of all of the different outcomes. A **Marginal Distribution** answers a slightly different question: given some value of one of the variables, what are the probabilities of the other variables?

When the variables are independent then the marginal distribution does not change from the joint distribution. Consider a simple example of X and Y discrete variables. X takes on values of 1 or 2 with probabilities of 0.6 and 0.4 respectively. Y takes on values of 1, 2, or 3 with probabilities of 0.5, 0.3, and 0.2 respectively. So we can give a table like this:

		5
	X=1 (60%)	X=2 (40%)
Y=1 (50%)	(1,1) at probability 0.3	(2,1) at probability 0.2
Y=2 (30%)	(1,2) at probability 0.18	(2,2) at probability 0.12
Y=3 (20%)	(1,3) at probability 0.12	(2,3) at probability 0.08

On the assumption that X and Y are independent. The probabilities in each box are found by multiplying the probability of each independent event.

If instead we had the two variables, A and B, not being independent then we might have a table more like this:

	A=1	A=2
B=1	(1,1) at probability 0.25	(2,1) at probability 0.13
B=2	(1,2) at probability 0.23	(2,2) at probability 0.12
B=3	(1,3) at probability 0.17	(2,3) at probability 0.1

We will examine the differences.

If we add up the probabilities along either rows or columns then we get the **marginal probabilities** (which we write in the *margins*, appropriately enough). Then we'd get:

	X=1 (60%)	X=2 (40%)	
Y=1 (50%)	(1,1) at probability 0.3	(2,1) at probability 0.2	0.5
Y=2 (30%)	(1,2) at probability 0.18	(2,2) at probability 0.12	0.3
Y=3 (20%)	(1,3) at probability 0.12	(2,3) at probability 0.08	0.2
	0.6	0.4	

Which just re-states our assumption that the variables are independent – and shows that, where there is independence, the probability of either variable alone does not depend on the value that the other variable takes on. In other words, knowing X does not give me any information about the value that Y will take on, and vice versa.

If instead we do this for the A,B case we get:

	A=1	A=2	
B=1	(1,1) at probability 0.25	(2,1) at probability 0.13	0.38
B=2	(1,2) at probability 0.23	(2,2) at probability 0.12	0.35

B=3 (1,3) at probability 0.17 (2,3) at probability 0.1 0.27 0.65 0.35

Where we double check that we've done it right by seeing that the sum of either of the marginals is equal to one (65% + 35% = 100% and 38% + 35% + 27% = 100%).

So the marginal distributions sum the various ways that an outcome can happen. For example, we can get A=1 in any of 3 ways: either (1,1), (1,2) or (1,3). So we add the probabilities of each of these outcomes to find the total chance of getting A=1.

But if we want to understand how A and B are related, it might be more useful to consider this as a prediction problem: would knowing the value that A takes on help me guess the value of B? Would knowing the value that B takes on help me guess the value of A?

These are abstract questions but they have vitally important real-life analogs. In airport security, is the probability that someone is a terrorist independent of whether they are Muslim? Is the probability that someone is pulled out of line for a thorough search independent of whether they are Muslim? *(The TSA might have different beliefs than you or me!)* In medicine, is the probability that someone gets cancer independent of whether they eat lots of vegetables? In economics, is the probability that someone defaults on their mortgage independent of the mortgage originator (Fannie, Freddie, mortgage broker, bank)? Is the probability of the country pulling out of recession independent of whether the Fed raises rates? In poker, if my opponent just raised the bid, what is the probability that her cards are better than mine?

For these questions we want to find the conditional distribution: what is the probability of some outcome, given a particular value for some other random variable?

Just from the phrasing of the question, you should be able to see that if the two variables are independent then the conditional distribution should not change from the marginal distribution – as is the case of X and Y. Flipping a coin does not help me guess the outcome of a roll of the dice. (Cheering in front of a sports game on TV does not affect the outcome, for another example – although plenty of people might dispute that!)

How do we find the conditional distribution? Take the value of the joint distribution and divide it by the marginal distribution of the relevant variable.

For example, suppose we want to find the probability of B outcomes, conditional on A=1. Since we know that A=1, there is no longer a 65% probability of A -- it happened. So we divide each joint probability by 0.65 so that the sum will be equal to 1. So the probabilities are now:

	A=1	A=2	
B=1	(1,1) at probability	(2,1) at probability 0.13	0.38
B=2	0.25/.65 (1,2) at probability 0.23/.65	(2,2) at probability 0.12	0.35

B=3	(1,3) at probability	(2,3) at probability 0.1	0.27
	0.17/.65 0.65/.65	0.35	
so now we get the cond	itional distribution:		
	A=1	A=2	
B=1	(1,1) @ 0.3846	(2,1) at probability 0.13	0.38
B=2	(1,2) @ 0.3538	(2,2) at probability 0.12	0.35
B=3	(1,3) @ 0.2615	(2,3) at probability 0.1	0.27
		0.35	

We could do the same to find the conditional distribution of B, given that A=2:

	A=1	A=2	
B=1	(1,1) at probability 0.25	(2,1) @ 0.13/.35 =.3714	0.38
B=2	(1,2) at probability 0.23	(2,2) @ 0.12/.35 =	0.35
B=3	(1,3) at probability 0.17 0.65	.3429 (2,3) @ 0.1/.35 = .2857	0.27

These conditional probabilities are denoted as $Pr\{B|A=2\}$ for example. We could find the expected value of B given that A equals 2, E[B|A=2], just by multiplying the value of B by its probability of occurrence, so $E[B|A=2] = (1 \cdot .3714) + (2 \cdot .3429) + (3 \cdot .2857)$.

We could find the conditional probabilities of A given B=1 or given B=2 or given B=3. In those cases we would sum across the rows rather than down the columns.

These are examples of what is called **Bayes' Theorem**:

$$P\left\{B\left|A\right\} = \frac{P\left\{A\left|B\right\} \cdot P\left\{B\right\}}{P\left\{A\right\}}$$

This can be understood by recalling the definition of conditional probability,

 $P\{A|B\} = \frac{P\{A \cap B\}}{P\{B\}}$, so $P\{B|A\} = \frac{P\{A \cap B\}}{P\{A\}}$, that the conditional probability equals the joint

probability divided by the marginal probability.

The power of Bayes' Theorem can be understood by thinking about medical testing. Suppose a genetic test screens for some disease with 99% accuracy. Your test comes back positive – how worried should you be? The surprising answer is not 99% worried; in fact often you might be more than likely to be healthy! Suppose that the disease is rare so only 1 person in 1000 has it (so 0.1%). So out of 1000 people, one person has the disease and the test is 99% likely to identify that person. Out of the remaining 999 people, 1% will be misidentified as having the disease, so this is 9.99 – call it 10 people. So eleven people will test positive but only one will

actually have the disease so the probability of having the disease given that the test comes up

positive,
$$P\{sick | test +\}$$
, is $\frac{P\{test + | sick\}P\{sick\}}{P\{test +\}} = \frac{0.99 \cdot 0.001}{0.01} = .099$.

The test is not at all useless – it has brought down an individual's likelihood of being sick by orders of magnitude, from one-tenth of one percent to ten percent. But it's still not nearly as accurate as the "99%" label might imply.

Many healthcare providers don't quite get this and explain it merely as "don't be too worried until we do further tests." But this is one reason why broad-based tests can be very expensive and not very helpful. These tests are much more useful if we first narrow down the population of people who might have the disease. For example home pregnancy tests might be 99% accurate but if you randomly selected 1000 people to take the test, you'd find many false positives. Some of those might be guys (!) or women who, for a variety of reasons, are not likely to be pregnant. The test is only useful as one element of a screen that gets progressively finer and finer.

Counting Rules

If A can occur as N_1 events and B can be N_2 events then the sample space is $N_1 \cdot N_2$ (visualize a contingency table with N_1 rows and N_2 columns).

Factorials: If there are N items then they can be arranged in

$$N! = (n)(n-1)(n-2)...(1) = \prod_{i=0}^{N-1} (N-i)$$
 ways.

Permutations: n events that can occur in r items (where order is important) have a total of

$$nPr = \frac{n!}{(n-r)!}$$
 possible outcomes.

Combinations: n events that can occur in r items (where order is not important) have $nCr = \frac{n!}{r!(n-r)!}$ possible outcomes – just the permutation divided by r! to take care of the multiple ways of ordering.

So to apply these, consider computer passwords (see NYTimes article below).

The article reports:

Mr. Herley, working with Dinei Florêncio, also at Microsoft Research, looked at the password policies of 75 Web sites. ... They reported that the sites that allowed relatively weak passwords were busy commercial destinations, including PayPal, Amazon.com and Fidelity Investments. The sites that insisted on very complex passwords were mostly government and university sites. What accounts for the difference? They suggest that "when the voices that advocate for usability are absent or weak, security measures become needlessly restrictive."

Consider the simple mathematics of why a government or university might want complex passwords. How many permutations are possible if passwords are 6 numerical digits? How many if passwords are 6 alphabetic or numeric characters? If the characters are alphabetic, numeric, and fifteen punctuation characters (, _ _ - ? ! (a) # \$ $\% ^ & * '$ ")? What if passwords are 8 characters? If each login attempt takes 1/100 of a second, how many seconds of "brute-force attack" does it take to access the account on average? If there is a penalty of 10 minutes after 3 unsuccessful login attempts, how long would it take to break in? (Of course, the article notes, if password requirements are so arcane that employees put their passwords on a Post-It attached to the monitor, then the calculations above are irrelevant.)

September 4, 2010

A Strong Password Isn't the Strongest Security

By RANDALL STROSS; New York Times

MAKE your password strong, with a unique jumble of letters, numbers and punctuation marks. But memorize it — never write it down. And, oh yes, change it every few months.

These instructions are supposed to protect us. But they don't.

Some computer security experts are advancing the heretical thought that passwords might not need to be "strong," or changed constantly. They say onerous requirements for passwords have given us a false sense of protection against potential attacks. In fact, they say, we aren't paying enough attention to more potent threats.

Here's one threat to keep you awake at night: Keylogging software, which is deposited on a PC by a virus, records all keystrokes — including the strongest passwords you can concoct — and then sends it surreptitiously to a remote location.

"Keeping a keylogger off your machine is about a trillion times more important than the strength of any one of your passwords," says Cormac Herley, a principal researcher at <u>Microsoft</u> Research who specializes in security-related topics. He said antivirus software could detect and block many kinds of keyloggers, but "there's no guarantee that it gets everything."

After investigating password requirements in a variety of settings, Mr. Herley is critical not of users but of system administrators who aren't paying enough attention to the inconvenience of making people comply with arcane rules. "It is not users who need to be better educated on the risks of various attacks, but the security community," he said at <u>a meeting of security professionals</u>, the <u>New Security Paradigms Workshop</u>, at Queen's College in Oxford, England. "Security advice simply offers a bad cost-benefit tradeoff to users."

One might guess that heavily trafficked Web sites — especially those that provide access to users' financial information — would have requirements for strong passwords. But it turns out that password policies of many such sites are among the most relaxed. These sites don't publicly discuss security breaches, but Mr. Herley said it "isn't plausible" that these sites would use such policies if their users weren't adequately protected from attacks by those who do not know the password.

Mr. Herley, working with Dinei Florêncio, also at Microsoft Research, looked at the password policies of 75 Web sites. At the Symposium on Usable Privacy and Security, held in July in Redmond, Wash., <u>they reported</u> that the sites that allowed relatively weak passwords were busy commercial destinations, including PayPal, <u>Amazon.com</u> and Fidelity Investments. The sites that insisted on very complex passwords were mostly government and university sites. What accounts for the difference? They suggest that "when the voices that advocate for usability are absent or weak, security measures become needlessly restrictive."

Donald A. Norman, a co-founder of the <u>Nielsen Norman Group</u>, a design consulting firm in Fremont, Calif., makes a similar case. In <u>"When Security Gets in the Way.</u>" an essay published last year, he noted the password rules of <u>Northwestern University</u>, where he then taught. It was a daunting list of 15 requirements. He said unreasonable rules can end up rendering a system less secure: users end up writing down passwords and storing them in places that can be readily discovered.

"These requirements keep out the good guys without deterring the bad guys," he said.

Northwestern has reduced its password requirements to eight, but they still constitute a challenging maze. For example, the password can't have more than four sequential characters from the previous seven passwords, and a new password is required every 120 days.

By contrast, <u>Amazon</u> has only one requirement: that the password be at least six characters. That's it. And hold on to it as long as you like.

A short password wouldn't work well if an attacker could try every possible combination in quick succession. But as Mr. Herley and Mr. Florêncio note, commercial sites can block "brute-force attacks" by locking an account after a given number of failed log-in attempts. "If an account is locked for 24 hours after three unsuccessful attempts," they write, "a six-digit PIN can withstand 100 years of sustained attack."

Roger A. Safian, a senior data security analyst at Northwestern, says that unlike Amazon, the university is unfortunately vulnerable to brute-force attacks in that it doesn't lock out accounts after failed log-ins. The reason, he says, is that anyone could use a lockout policy to try logging in to a victim's account, "knowing that you won't succeed, but also knowing that the victim won't be able to use the account, either." (Such thoughts may occur to a student facing an unwelcome exam, who could block a professor from preparations.)

VERY short passwords, taken directly from the dictionary, would be permitted in a password system that Mr. Herley and Stuart Schechter at Microsoft Research developed with Michael Mitzenmacher at Harvard.

At the Usenix Workshop on Hot Topics in Security conference, held last month in Washington, the three suggested that Web sites with tens or hundreds of millions of users, could let users choose any password they liked — as long as only a tiny percentage selected the same one. That would render a list of most often used passwords useless: by limiting a single password to, say, 100 users among 10 million, the odds of an attacker getting lucky on one attempt per account are astronomically long, Mr. Herley explained in a conversation last month.

Mr. Herley said the proposed system hadn't been tested and that users might become frustrated in trying to select a password that was no longer available. But he said he believed an anything-is-permitted password system would be welcomed by users sick of being told, "Eat your broccoli; a strong password is good for security."

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